Forecasting the Growth of Complexity and Change

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ABSTRACT

In the spirit of punctuated equilibrium, complexity is quantified relatively in terms of the spacing between equally important evolutionary turning points (milestones). Thirteen data sets of such milestones, obtained from a variety of scientific sources, provide data on the most important complexity jumps between the big bang and today. Forecasts for future complexity jumps are obtained via exponential and logistic fits on the data. The quality of the fits and common sense dictate that the forecast by the logistic function should be retained. This forecast stipulates that we have already reached the maximum rate of growth for complexity, and that in the future complexity's rate of change (and the rate of change in our lives) will be declining. One corollary is that we are roughly halfway through the lifetime of the Universe. Another result is that complexity's rate of growth has built up to its present high level via seven evolutionary sub processes, themselves amenable to logistic description.

1. Introduction

Change has always been an integral feature of life. "You cannot step twice in the same river", said Heraclitus—who has been characterized as the first Western thinker—illustrating the reality of permanent change. Heraclitus invoked an incontrovertible law of nature according to which everything is mutable, "all is flux." In the physics tradition such laws are called universal laws, for example, the second law of thermodynamics, which stipulates that entropy always increases, and explains such things as why there can be no frictionless motion. In fact, there are theories that link the accumulation of complexity to the dissipation of entropy, or wasted heat.

The accelerating amount of change in technology, medicine, information exchange, and other social aspects of our life, is familiar to everyone. Progress—questionably linked to technological achievements—has been following progressively increasing growth rates. The exponential character of the growth pattern of change is not new. Whereas significant developments for mankind crowd together in recent history, they populate sparsely the immense stretches of time in the earlier world. The marvels we witnessed during the 20th century surpass what happened during the previous one thousand years, which in turn is more significant than what took place during the many thousands of years that humans lived in hunting-gathering societies. What is new is that we are now reaching a point of impasse, where change is becoming too rapid for us to follow. The amount of change we are presently confronted with is approaching the limit of the untenable. Many of us find it increasingly difficult to cope effectively with an environment that changes too rapidly.

What will happen if change continues at an accelerating rate? Is there a precise mathematical law that governs the evolution of change and complexity in the Universe? And if there is one, how *universal* is it? How long has it been in effect and how far in the future can we forecast it? If this

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law follows a simple exponential pattern, we are heading for an imminent singularity, namely the absurd situation where change appears faster than we can become aware of it. If the law is more of a natural-growth process (logistic pattern), then we cannot be very far from its inflection point, the maximum rate of change possible.

2. The Task

Change is linked to complexity. Complexity increases both when the rate of change increases and when the amount of things that are changing around us increase. Our task then becomes to quantify complexity, as it evolved over time, in an objective, scientific and therefore defensible way. Also to determine the law that best describes complexity's evolution over time, and then to forecast its future trajectory. This will throw light onto what one may reasonably expect as the future rate at which change will appear in society.

However, quantifying complexity is something easier said than done.

COMPLEXITY

We have seen much literature and extensive preoccupation of "hard" and "less hard" scientists with the subject of complexity. Yet we have neither a satisfactory definition for it, nor a practical way to measure it. The term complexity remains today vague and unscientific. In his best-selling book *Out of Control* Kevin Kelly concludes:[1]

How do we know one thing or process is more complex than another? Is a cucumber more complex than a Cadillac? Is a meadow more complex than a mammal brain? Is a zebra more complex than a national economy? I am aware of three or four mathematical definitions for complexity, none of them broadly useful in answering the type of questions I just asked. We are so ignorant of complexity that we haven't yet asked the right question about what it is.

But let us look more closely at some of the things that we do know about complexity today:

- It is generally accepted that complexity increases with evolution. This becomes obvious when we compare the structure of advanced creatures (animals, humans) to primitive life forms (worms, bacteria).
- It is also known that evolutionary change is not gradual but proceeds by jerks. In 1972 Niles Eldredge and Stephen Jay Gould introduced the term "Punctuated Equilibria": long periods of changelessness or *stasis*—equilibrium—interrupted by sudden and dramatic brief periods of rapid change—punctuations.[2]

These two facts taken together imply that complexity itself must grow in a stepladder fashion, at least on a macroscopic scale.

- Another thing we know is that complexity begets complexity. A complex organism creates a niche for more complexity around it; thus complexity is a positive feedback loop amplifying itself. In other words, complexity has the ability to "multiply" like a pair of rabbits in a meadow.
- Complexity links to connectivity. A network's complexity increases as the number of connections between its nodes increases, and this enables the network to evolve. But you can have too much of a good thing. Beyond a certain level of linking density, continued connectivity decreases the adaptability of the system as a whole. Kauffman calls it "complexity catastrophe": an overly linked system is as debilitating as a mob of uncoordinated loners.[3]

These two facts argue for a process similar to growth in competition. Complexity is endowed with a multiplication capability but its growth is capped and that necessitates some kind of a selection mechanism. Alternatively, the competitive nature of complexity's growth can be sought in its intimate relationship with evolution. One way or another, it is reasonable to expect that complexity follows logistic-growth patterns as it grows.

MILESTONES IN THE HISTORY OF THE COSMOS

The first thing that comes to mind when confronted with the image of stepwise growth for complexity over time is the major turning points in the history of evolution. Most teachers of biology, biochemistry, and geology at some time or another present to their students a list of major events in the history of life. The dates they mention invariably reflect milestones of punctuated equilibrium (or "punk eek" for short). Physicists tend to produce a different list of dates stretching over another time period with emphasis mostly on the early Universe.

Such lists constitute data sets that may be plagued by numerical uncertainties and personal biases depending on the investigator's knowledge and specialty. Nevertheless the events listed in them are "significant" because some investigator has singled them out as such among many others. Consequently they constitute milestones that can in principle be used for the study of complexity's evolution over time. However, in practice there are some formidable difficulties in producing a data set of turning points that cover the entire period of time (15 billion years).

I made the bold hypothesis that a law has been in effect *from the very beginning*. This was not an arbitrary decision on my part. The suggestion came when I first looked at an early compilation of milestones. In any case, I knew that confrontation with real data would be my final judge. More than once in this paper I have turned to the scientific method as defined by experimental physicists, namely: Following an observation (or hunch), make a hypothesis, and see if it can be verified by real data.

THE CHALLENGES

Here are the most challenging issues concerning this paper's methodology in order of decreasing importance, and the way they were dealt with:

1. The complexity associated with a milestone must be quantified at least in relative terms. For example, how much complexity did the Cambrian explosion bring to the system compared to the amount of complexity added to the system when humans acquired speech?

To quantify the complexity associated with an evolutionary milestone we must look at the milestone's importance. *Importance* can be defined as equal to *the change in complexity multiplied by the time duration to the next milestone*. This definition has been derived in the classical physics tradition: you start with a magnitude (in our case *Importance*), you put an equal sign next to it, and then you proceed to list in the numerator whatever the quantity in question is proportional to, and in the denominator whatever it is inversely proportional to, keeping track of possible exponents and multiplicative constants. It is intuitively obvious that for a milestone *Importance* is linearly proportional to the amount of complexity added by the milestone, and also linearly proportional to how long the system survives unchanged following the milestone. The greater the complexity jump at a given milestone, or the longer the ensuing stasis, the greater the milestone's importance will be.

Importance = Complexity x Duration (1)

The complexity change associated with a certain milestone will then be inversely proportional to the time period to the next milestone. And to the extent that we are considering milestones of *comparable* importance, we have a means of quantitatively comparing the change in complexity associated with each jump.

Following each milestone the complexity of the system increases by certain amount. At the next milestone there is another increase in complexity. Assuming that milestones are approximately of equal importance, and according to the above definition of importance we can conclude that the increase in complexity ΔC_i associated with milestone i of importance I is

$$\Delta C_i = \frac{1}{\Delta T_i}$$
(2)

where ΔT_i the time period between milestone i and milestone i+1.

We thus have a relative measure of the complexity contributed by each milestone to the system. If milestones become progressively crowded together with time, their complexity is expected to become progressively larger, see Figure 1.

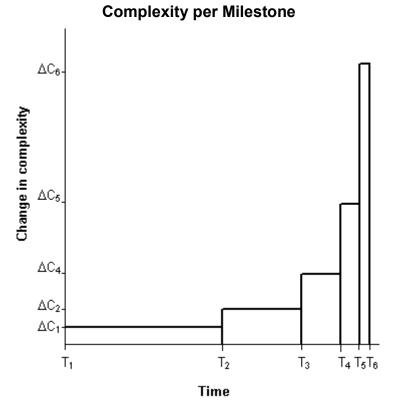


Figure 1. To the extent that milestones of equal importance appear more frequently, their respective complexity increases. The area of each rectangle represents importance and remains constant. The scales of both axes are linear.

2. The time frame is vast and the crowding of milestones in recent times is so dense that no logistic or exponential function can be used to describe the growth process.

A logistic function does not necessarily need to be a function of time. Moreover, there are processes for which our Euclidean conception of time is not appropriate. For this analysis a better-suited time variable is the sequential milestone number because this way we can handle the singularity as $\Delta T \rightarrow 0$. Once forecasts are obtained for complexity jumps associated with future

milestones we can use the definition of importance coupled with the equi-importance assumption to derive explicit dates for future milestones.

3. Milestones from different evolutionary processes (cosmological, geological, biological, etc.) and by different authors (physicists, biologists, historians, etc.) need to be combined in a rigorous way. There is a need for normalization when authors furnish data sets with different numbers of milestones for the same chronological period.

The equi-importance assumption is key to dealing with both of these issues. If all milestones in a data set are equally important, then the corresponding complexity jumps—calculated as described in Challenge 1—are directly comparable no matter what evolutionary process they belong to. Similarly, if someone's data set contains more milestones that someone else's data set for the same chronological period, then the milestones in the former set must carry less importance than those in the latter. The data sets are normalized so that they give the same overall complexity contribution for the same time periods.

4. How many turning points should an adequate data set contain? One can always argue that a large number of important events have been neglected.

If we consider only the top most important milestones, we can invoke Pareto's rule—also known as the 80/20 rule—to argue that 20 percent of all milestones account for 80 percent of all complexity acquired during the time period in question. Moreover dealing with only major milestones improves the equi-importance requirement. Milestones of *large* importance are by definition milestones of *comparable* importance. Naturally some of them will be more important than others, but the average importance will be a relatively large number, and the spread around this average a relatively small number. Therefore, on a first approximation we can treat all milestones as being of *equal* importance.

<u>Remark:</u> A milestones is assigned to a point in time, i.e. a date. If more than one event is associated with the same date, the milestone's importance reflects the sum total of the importance of all such events.

3. The Data

My first attempt to compile a set of milestones and determine a growth law from it turned out bittersweet. I analyzed 20 milestones compiled during a brainstorming session with colleagues. This early data set proved amenable to a description by a logistic curve, but the result was subsequently criticized on the ground that there could be bias in the choice of milestones. So I set out to find more objective data from independent and reliable sources in order to be able to defend them as unbiased.

Searching the Internet for something like "Major Events in the History of..." yields scores of pointers and chronologies so-called timelines. Many of them have to do with some classroom assignment. Some of them stand out in terms of completeness and credibility. I briefly present below six of the thirteen data sets I have retained. A complete list of the data used in the analysis, including milestone descriptions and dates, can be found in Appendix A.

• The Cosmic Calendar. Carl Sagan has put together a one-year calendar matching the entire history of the Universe, and pointing out dates of major events.[4] The set consists of 47 milestones that cover the entire time period (big bang to present) but suffer somewhat from the calendar format. Time resolution becomes insufficient for milestones that fall in the same time bucket. It happens with the calendar's monthly buckets, and again later with the buckets of seconds. In fact, it seems that during these periods of saturated time resolution Sagan is

enumerating milestones on a bucket-by-bucket basis reporting on things that happened during the time bucket, as if he is driven by the structure of the time buckets instead of the spacing of the events.

- The data sets from Encyclopedia Britannica and the A.M.N.H. (American Museum of Natural History) are free from time-resolution distortions but are less exhaustive. They contain 16 and 20 milestones respectively.
- Major Events in the History of Life. More than 1700 students, faculty, and other members of the UCLA community attended a "Major Events in the History of Life" symposium on January 11, 1991, convened by the IGPP Center for Study of Evolution and the Origin of life at the University of California. A volume was put together making accessible the proceedings of that symposium.[5]
- **Major Events in the Universe's History.** Two physicists published a *Scientific American* article entitled "The Structure of the Early Universe." Their data set concerns events and dates covering the pre-human evolution of the universe.[6]
- Professor Paul D. Boyer, biochemist, Nobel Prize 1997, kindly provided me with his own set of milestones for which I assigned the dates.

The data used in the analysis incorporate milestones from thirteen data sets, the last of which is the author's own. I decided to include a data set of my own for two reasons. First, I believe that having gone through all the research, I was well positioned to distill a rather complete, defensible, and scientific set of evolutionary milestones. Second, I needed data on the twentieth century, neglected by the other authors. From the 12 sets considered only Sagan's data set addresses the twentieth century, and his data are plagued by the calendar-format problem mentioned earlier.

From the 13 data sets only Paul Boyer's and mine were created in direct response to the question: Which are the 25 most significant milestones in the evolution of the Universe? The motivation of other authors, like Sagan and A.M.N.H., was to put events into a time perspective. But in so doing, they answered the same question simply by selecting what to list as major events.

Because of the different number of milestones between data sets, and the fact that different sets sometimes give different dates for the same event (e.g., the time of the big bang ranges from 13 to 20 billion years ago), I decided to derive a "canonical" set of milestones and use the spread between authors to calculate errors. My assumption was that there must be some coherence between the 13 data sets, i.e., many milestone dates must be common to most sets. Combining 13 data sets into one greatly reduces the uncertainties on the results.

THE CANONICAL SET OF MILESTONES

Figure 2 shows a histogram of all milestone dates (a total of 302) with logarithmically increasing time buckets as we go backward in time. This choice of binning the data is not arbitrary. It became obvious when I plotted the 302 points on a number of linear graphs with different-size time buckets each. The logarithmically increasing time buckets are chosen in such a way that each bucket receives one cluster of milestones. The peak of each cluster is used to define a date for a milestone of the canonical set used as time variable in our analysis. There are twenty-eight canonical milestones but because of complexity's definition (Equation 2) there only twenty-seven peaks in Figure 2.

For each peak the average complexity change is calculated, as well as an error given by the spread around the peak (one standard deviation). For peaks featuring only one entry (for example, milestones during the last 100 years) I arbitrarily assign the average error as error. Fractional milestone numbers are assigned to all milestones according to their date.

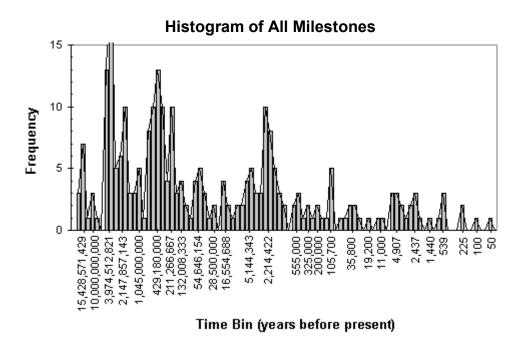


Figure 2. A histogram of all milestones with logarithmic time buckets. The thin black line is superimposed to outline the peaks that define the dates of the "canonical" milestones. On the horizontal axis we read the dates of these milestones.

4. The Analysis

A distribution of the change of complexity per milestone for all thirteen data sets is shown in Figure 3. The different data sets have been normalized for equal cumulative complexity contributions over identical time periods. Consequently the units of the vertical axis are arbitrary to an overall multiplicative constant. The picture comparing the normalized data for all thirteen sources is rather coherent as there is good agreement between the different data sets. Furthermore the data points generally line up on a straight line in a semi-log plot, which is the hallmark of exponential growth, or alternatively, the early part of logistic growth. The milestone-number axis marks the milestones of the canonical set.

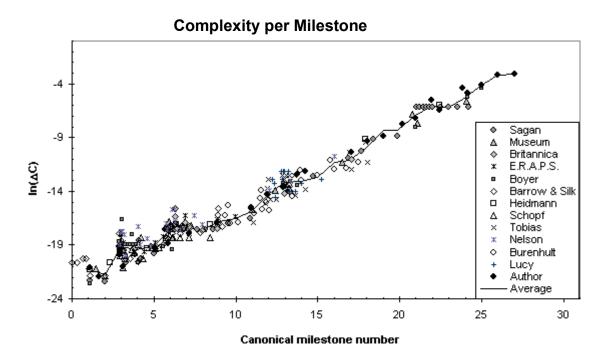


Figure 3. Thirteen different sources of data corroborate each other. The thin black line connects the canonical milestones (see text), and also represents the average complexity change at a given milestone. The vertical axis depicts the logarithm of the change in complexity.

We can now proceed to fit the data with an exponential and a logistic function. Given that Figure 3 depicts complexity's *rate of growth*—i.e., complexity change per milestone—we expect the trend to follow the *first derivative* of the two functions. We therefore fit to the expressions:

 $e^{(\alpha X + \beta)}$

where α and β constants, and where M, α , and \mathbf{x}_{o} constants

ln(logistic life cycle)

$$\ln\left\{\frac{M\alpha}{(1+e^{-\alpha(X-Xo)})\cdot(1+e^{\alpha(X-Xo)})}\right\}$$

and x the sequential milestone number. The logistic life cycle is the first derivative of the familiar logistic function:

Figure 4 shows the canonical set of milestones with an exponential and a logistic fit superimposed. The logistic fit is better than the exponential one, (70% confidence level compared to 30%). Table I shows the particular details of the fits.

Table 1 - Fit Results						
Formula fit	α	Μ	Xo	χ^2	Degrees of freedom	
(αΧ+β)	-23.749	0.7554			28.3	25
$\ln \left\{ \frac{M\alpha}{(1+e^{-\alpha(X-Xo)})/(1+e^{\alpha(X-Xo)})} \right\}$	xo)) }	0.7735	0.1375	27.89	20.2	24

Table I - Fit Results

I have made an attempt to be scientifically correct. However, the reader should be aware that the Chi-square estimates (and the associated confidence levels) cannot reflect all uncertainties. There are sources of error that have not been properly accounted for. For example, errors due to having

widely different dates for the same event (sometimes with good reason as the exact date is still being debated), or errors due to the approximation that the milestones are equally important.

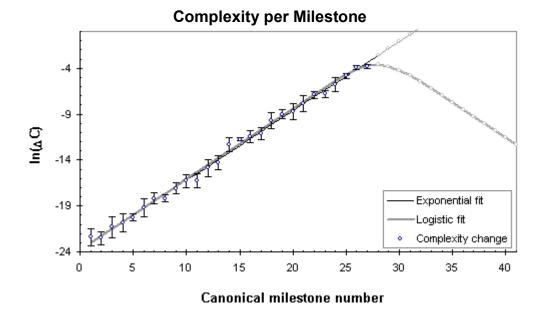


Figure 4. Logistic and exponential fits to the data of the canonical milestone set. The vertical axis depicts the logarithm of the change in complexity. The faint circles on the forecasted trends indicate the complexity of future milestones.

The mid point of the logistic function is milestone number 27.89, which corresponds to 10 years ago. In other words, complexity grew at the highest rate ever around 1990. From then onward complexity's rate of change began decreasing. Future milestones of comparable importance will henceforth be appearing less frequently.

But according to the exponential law, milestones punctuating complexity jumps will continue appearing closer together at the same exponential rate, and 25 years from now we should expect successive turning points of the same importance to be spaced only 5 days apart. Table II spells out the timing of future milestones as expected from the logistic and exponential growth laws determined by the above fits.

Table 11 - Forecasts for Complexity Change as a Function of Time				
Milestone	Logistic	Exponential fit		
number	Complexity change*	Years from now	Complexity change *	Years from now
28	0.0265	38	0.0744	13.4
29	0.0223	45	0.1584	6.3
30	0.0146	69	0.3372	3.0
31	0.0081	124	0.7178	1.4
32	0.0041	245	1.5278	0.7
33	0.0020	508	3.2518	0.3
34	0.0009	1078	6.9213	0.1
35	0.0004	2315	14.7317	0.07
36	0.0002	5000	31.3558	0.03
37	0.0001	10800	66.7397	0.015

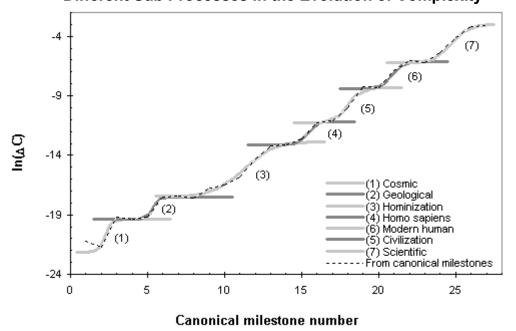
Table II - Forecasts for Complexity Change as a Function of Time

* In the same arbitrary units as Figures 3 and 4.

The accuracy of the results, as reflected in the significant digits retained in the numbers reported, may seem overly optimistic. However, the reader should bear in mind two things. First, that the curves are extremely steep; on linear time scale they would appear practically horizontal across billions of early-Universe years. Second, the significant digits in the results reflect more the *precision* of the method and less the *accuracy* of the answers because not all systematic errors have been accounted for (see earlier remark on sources of unaccounted errors). THE CLOSE-UP PICTURE

The case can be made, if less rigorously, for a finer structure in the evolution of the trajectory of complexity's change. It is has been shown that any growth processes may consist of smaller logistic sub-processes.[7] Looking at Figure 3 closely we can discern smaller S-shaped steps. Such structure indicates an alternation between periods when the milestones progressively crowd together and periods when they are roughly regularly spaced in time. This is largely due to the fact that as we move through time we encounter a number of rather well defined evolutionary sub processes. The thin black line in Figure 3 (representing the average change of complexity per milestone), suggests at least seven such sub processes. In figure 5 logistic curves are adapted to these segments.

The seven logistic curves do not result from rigorous fits to the data because of too few milestones and too much jitter on the data points in each segment (otherwise said, too large errors for the fitting procedure to work). The thick gray lines are logistic functions drawn in to simply guide the eye. However, the fair agreement between thick lines and the corresponding sections of the dotted line is evidence that we are dealing with rather independent natural-growth processes.



Different Sub Processes in the Evolution of Complexity

Figure 5. Seven small logistic curves have been superimposed to point out evidence for a finer structure. The dotted line is the same as the thin black line in Figure 3. The vertical axis depicts the logarithm of the change in complexity. The legend lists the sub processes in chronological order.

In order to better understand the seven sub processes, Table III lists the relevant parameters for each process. The mathematical parameters of the logistic functions being of less interest, it is preferable to give the dates corresponding to the 10%, 50%, and 90% penetration level for each

process. The range 10%-90% of a logistic growth process is traditionally taken as the period of main thrust toward higher growth. Above the 90% level one can argue that a stable maximum level has been reached.

Table III - The Seven Thases of Complexity's Growth			
Evolutionary process	10%	50%	90%
	Y	ears before presen	t
Cosmic	13,100,000,000	10,100,000,000	7,900,000,000
Geological	1,450,000,000	1,050,000,000	820,000,000
Hominization	19,500,000	4,020,000	625,000
Homo sapiens	434,000	308,000	239,000
Modern human	107,000	38,200	15,100
Civilization	10,700	6,130	5,000
Scientific	539	225	100

Table III - The Seven Phases of Complexity's Growth

The names given to the seven phases have been inspired by what happened during each sub process. Consequently, "Cosmic" refers to the process around the formation of our galaxy. "Geological" refers to early forms of life and is centered on the appearance of multicellular life. "Hominization" is the period between the divergence of orangutan from Hominidae and the development of speech; it is centered on the appearance of first bipedalism and stone tools. "Homo sapiens" is a relatively short period dominated by Homo sapiens and the domestication of fire. "Modern human" extends between the first burial of the dead and the invention of agriculture; it is centered around the time of rock art, and includes ritual/spiritual behavior (magic shamanism). "Civilization" is a name inspired by city dwelling and religion becoming important; it is centered around the appearance of writing and the wheel. Finally, "Scientific" is the growth phase that begins with renaissance, and ends with modern physics; it is centered on the industrial revolution, and the establishment of scientific method.

5. Discussion of Results

This paper studies the evolution of complexity from the beginning of the Universe to present day. The hypothesis, verified via a successful logistic fit on data, is that a simple diffusion law has been governing complexity's growth across divers evolutionary processes (cosmological, geological, biological, etc.). We are obviously concerned with an anthropic Universe here since we are overlooking how complexity has been evolving in other parts of the Universe. Still, the author believes that such an analysis carries more weight than just the elegance and simplicity of its formulation. John Wheeler has argued that the very validity of the laws of physics depends on the existence of consciousness.² In a way, the human point of view is all that counts!

The work reported here links logistic growth and complexity in two different ways. One way is how complexity has been accumulating in the Universe along a large logistic curve (Figure 4). Another way is how complexity's rate of growth has been following smaller logistic curves in the close-up picture of Figure 5. There is a fundamental difference between these two pictures. The former involves an S-shaped pattern fitted to the amount of *change accumulated* whereas the latter involves fitting S-shaped patterns to the *rate of change*. In both cases evidence for logistic growth argues for natural growth in competition (Darwinian in nature), but the interpretations are different.

SEEING COMPLEXITY AS A COMPETITIVE GROWTH PROCESS

² John Wheeler is professor at Princeton University and presently director of the Center for Theoretical Physics at the University of Texas, Austin.

Observation of logistic growth enables one to argue for the existence of Darwinian competition. Such competition implies that:

- Some "species" is capable of growing via multiplication.
- Members of the "species" compete for a limited resource.
- There is natural selection.

In the logistic function of Figure 4 the "species" is the system's complexity and its members are the complexity chunks carried by the milestones. The limited resource is the system's cumulated final complexity. It is limited because too much complexity may hurt survival as per Kauffman's argument for complexity catastrophe mentioned earlier.

In the logistic functions of Figure 5 the "species" is the speed with which each evolutionary sub process proceeds, and its members are the jumps in speed during the rapid-growth phase (when turning points appear progressively more frequently). The limited resource is maximum speed, characteristic of the evolutionary sub process in question (e.g., geological evolution reached higher levels of complexity per milestone than cosmic evolution).

There is selection everywhere. Changes, be it in complexity, or in the rate of growth of complexity, are like mutants; only the best-fit ones survive. Potential changes lurk around like potential accidents, waiting for the opportunity to become realized. If a change represents too large or too small a step for the moment in history of the evolutionary process it belongs to, it will not survive (i.e., it will not become realized). At the same time, if the system's cumulated complexity approaches saturation—some billion years from now—changes, and the evolutionary sub process they belong to, will have to be confined to miniscule sizes. Big mutations at that point in time will simply have no chance of being realized.

THE ULTIMATE S-CURVE

The large-scale logistic description of Figure 4 indicates that the evolution of complexity in the Universe has been following a logistic growth pattern from the very beginning, i.e. from the big bang. This is remarkable considering the vastness of the time scale, and also the fact that complexity resulted from very different evolutionary processes, for example, planetary, biological, social, and technological. The fitted logistic curve has its inflection point—the time of the highest rate of change—around 1990. Considering the symmetry of the logistic-growth pattern, we can thus conclude that the end of the Universe is roughly another 15 billion years away. Such a conclusion is not really at odds with the latest scientific thinking that places the end of the solar system some 5 billion years from now.

The ultimate S-curve of Figure 4 is not a function of time but of milestone number. The Sshaped pattern would be rather distorted if we plotted complexity as a function of time (very flat for billions of years and very steep at present). But the forecasts of complexity per future milestone can be translated to complexity per future date according to Equation (2). We therefore see from Table II that the next three milestones are due in 38, 45, and 69 years from now. To give some perspective we can look at the last three milestones:

- 5 years ago: Internet / human genome sequenced
- 50 years ago: DNA / transistor / nuclear energy
- 100 years ago: modern physics (radio, electricity, etc.) / automobile / airplane

In other words, dates for world-shaking milestone like the above three should be expected around 2038, and then again around 2083 and 2152.

INDEPENDENT CORROBORATION

During this paper's reviewing process one of the reviewers brought to my attention that Richard Coren has done a similar analysis on a set of 13 events he described as "critical transitions in evolution on Earth" in his book *The Evolutionary Trajectory*.[8] Coren looked at evolution in terms of information transfer, much like J. M. Smith and E. Szathmary did with their small set of six transitions.[9] I could not resist trying my approach on Coren's data set.

The logistic fit turned out excellent with a mid point around 1860 A.D. I consider this to be in exceptionally good agreement with my result (1990 A.D.) given that Coren's sampling is much coarser; his data set has less than half the data points I have in my canonical set. Data sets with few points, when individually analyzed, generally gave much poorer agreement. Moreover, in view of the earlier discussion on unaccounted systematic errors, such agreement must be considered as fortuitous. Nevertheless it brings certain corroboration.

For the sake of completeness Coren's data set, my logistic fit to it, and the corresponding graph are given in Appendix B.

OTHER INSIGHTS

According to the classification of Table III events like the Cambrian explosion are not the singular turning points purported to be. Once the Geological sub process was completed, important events continued to take place for a long stretch of time (almost 800 million years) at a maximum but rather *constant* rate. Cambrian explosion was one such event; others were:

- Appearance of invertebrates
- Plants colonized land
- Appearance of amphibians
- Appearance of insects
- Appearance of reptiles
- Mass extinction (trilobites)
- Appearance of dinosaurs and mammals
- Birds evolved from reptiles
- Appearance of flowering plants
- Asteroid collision and the ensuing mass extinction (including dinosaurs)

All these events took place between the end of Geological (around 800 million years ago) and the beginning of Hominization growth phases (around 20 million years ago), and are roughly of comparable time spacing (hence complexity) and importance.

Special significance has been attributed to the Cambrian explosion—and other events like the invention of agriculture, the discovery of DNA and nuclear energy, and Internet and the sequencing of the human genome—and yet they do not constitute turning points between distinct evolutionary growth processes but rather occupy the stretches of time characterized by uniform change between the end of one sub process and the beginning of the next one. Contrary to what one may have expected, complexity increased at a rather *constant* rate—albeit large—during the twentieth century. The major thrust forward of the scientific evolutionary process took place earlier, around the discovery of the steam engine.

A better identification for the seven evolutionary sub processes is provided by events that occupy the time period when the rate of growth of complexity underwent a sharp increase. These are events around the 50% points of Table III such as:

- Star formation (Cosmic)
- The appearance of multicellular life (Geological)
- First bipedalism and stone tools (Hominization)
- The domestication of fire (Homo sapiens)
- Rock art (Modern human)
- The appearance of writing and the discovery of the wheel (Civilization)
- The discovery of the steam engine (Scientific)

Another interesting observation in the close-up picture of Figure 5 is the miniscule rate of growth of complexity before significant life forms appeared (i.e., before hominization). This fact concords

with the well-accepted notion that there was no complex matter in the universe before life. According to astrochemists, we can't find complex molecules in the universe outside of life.

6. Sitting on Top of the World

Summarizing the conclusions we can say that the Universe's complexity has been growing along a large-scale logistic pattern that has just reached its mid point. In fact, the rate of complexity's growth has just reached its maximum, after having gone through seven steps each of which can itself be interpreted as a natural-growth sub process. As the rate of change begins declining, the next sub process is expected to be a downward step following an upside-down S-curve.

But the analysis of complexity's evolution also gave an exponential pattern—if with lower confidence level—as a possibility for the appearance of future milestones. For skeptics of logistics, those who advocate that complexity can continue growing exponentially, Table II tells us that the next milestone should be in 13.4 years, the following one in 6.3 years, the one after that in 3 years, and then again in 1.4 years, and so on. But the pattern becomes so steep that all future milestones are expected to appear in less than 26 years from now.³ In other words people who will still be alive in 2026—i.e., the generation of people born in the mid 1940s or later—will have witnessed before they die all the change that can ever take place!

Therefore, in addition to the goodness-of-fit argument, there is a common-sense argument that favors the logistic-law alternative. But the logistic life cycle also peaks during the lifetime of people born in the mid 1940s. In particular it spells out that we are presently traversing the only time in the history of the Universe in which 80 calendar years can witness change in complexity coming from as many as three evolutionary milestones. We happen to be positioned at the world's prime!

Coincidentally the mid 1940s is the time of the baby boom that creates a bulge on the population distribution. As if by some divine artifact a larger-than-usual sample of individuals was meant to experience this exceptionally turbulent moment in the evolution of the cosmos.

The author would like to thank Eric L. Schwartz, professor of Cognitive and Neural Systems at Boston University, for many useful discussions the first one of which led to the conception of this research work.

³ The pattern of a decaying exponential is asymptotic, i.e. it needs infinite time to reach zero, but its definite integral between x and ∞ is finite.

APPENDIX A

This appendix contains the raw data used in the paper. The first twelve data sets, provided by independent sources, influence to some extent the thirteenth data set compiled by the author. Milestones denote dates; consequently events occurring at the same time are represented by a single milestone.

1. The data set of Carl Sagan as outlined in his Cosmic Calendar.[4] The precise year numbers have been assigned by the author.

	Milestone	Years ago
1	Big Bang	1.5E+10
2	Origin of Milky Way Galaxy	1.0E+10
3	Origin of the Solar System	4.6E+09
	Formation of the Earth	4.4E+09
5	Origin of life on Earth	4.0E+09
6	Formation of the oldest rocks known on Earth	3.7E+09
7	Date of oldest fossils (bacteria and blue-green algae)	3.4E+09
8	Invention of sex (by microorganisms)	2.5E+09
9	Oldest fossil photosynthetic plants	2.0E+09
10	Eukaryotes (first cells with nuclei) flourish	1.9E+09
11	Significant oxygen atmosphere begins to develop on Earth	1.2E+09
12	Extensive volcanism and channel formation on Mars	1.0E+09
13	First worms	6.2E+08
14	Precambrian ends. Paleozoic Era and Cambrian Period begin. Invertebrates flourish	5.7E+08
15	First oceanic plankton. Trilobites flourish.	5.3E+08
16	Ordovician Period. First fish, first vertebrates.	4.9E+08
17	Silurian Period. First vascular plants. Plants begin colonization of land	4.5E+08
18	Devonian Period begins. First insects. Animals begin colonization of land	4.1E+08
19	First amphibians. First winged insects.	3.7E+08
20	Carboniferous Period. First trees. First reptiles.	3.3E+08
21	Permian Period begins. First dinosaurs.	2.9E+08
22	Paleozoic Era ends. Mesozoic Era Begins.	2.5E+08
23	Triassic Period. First mammals.	2.1E+08
24	Jurassic Period. First birds.	1.6E+08
25	Cretaceous Period. First flowers. Dinosaurs become extinct.	1.2E+08
26	Mesozoic Era ends. Cenozoic Era Tertiary Period begins. First cetaceans. First	
	primates.	8.2E+07
27	First evolution of frontal lobes in the brain of primates. First hominids. Giant	
	mammals flourish.	4.1E+07
28	Origin of Proconsul and Ramapithecus, probable ancestors of apes and men	1.8E+07
29	First humans	2.6E+06
30	Widespread use of stone tools	1.7E+06
31	Domestication of fire by Peking man	4.1E+05
32	Beginning of most recent glacial period	1.2E+05
33	Seafarers settle Australia	5.8E+04
34	Extensive cave painting in Europe	2.9E+04
35	Invention of agriculture	1.9E+04
36	Neolithic civilization; first cities	1.2E+04

37	First dynasties in Summer, Ebla, and Egypt; development of astronomy	4800
38	Invention of the alphabet; Akkadian Empire	4300
39	Hammurabic legal codes in Babylon; Middle Kingdom in Egypt	3800
40	Bronze metallurgy; Mycenaean culture; Trojan War; Olmec culture; invention of	
	the compass	3400
41	Iron metallurgy; First Assyrian Empire; Kingdom of Israel; founding of Carthage	
	by Phoenicia	2900
42	Asokan India; Ch'in Dynasty China; Periclean Athens; birth of Buddha	2400
43	Euclidian geometry; Archimedean physics; Ptolemaic astronomy; Roman Empire;	
	Christ	1900
44	Zero and decimals invented in Indian arithmetic; Rome falls; Moslem conquests	1400
45	Mayan civilization; Sung Dynasty China; Byzantine empire; Mongol invasion;	
	crusades	1000
46	Renaissance in Europe; voyages of discovery from Europe and from Ming Dynasty	
	China; emergence of the experimental method in science	500
47	Widespread development of science and technology; emergence of global culture;	
	acquisition of the means of self-destruction of the human species; first steps in	
	space craft planetary exploration and the search of extraterrestrial intelligence	0

2. The data set found in the American Museum of Natural History.[10] The precise date numbers have been provided by the author.

	Milestone	Years ago
1	Big Bang	1.3E+10
2	Milky Way forms	1.0E+10
3	Sun and planets form	4.5E+09
4	Oldest known life (single cell)	3.8E+09
5	First multicellular organisms	1.0E+09
6	Cambrian Explosion (burst of new life forms)	5.5E+08
7	Emergence of first vertebrates	4.8E+08
8	Early land plants	4.4E+08
9	Variety of insects begin to flourish	3.9E+08
10	First dinosaurs appear	2.3E+08
11	First mammalian ancestors appear	1.9E+08
12	First known birds	1.4E+08
13	Dinosaurs wiped out by asteroid or comet	6.5E+07
14	Apes appear	1.6E+07
15	First human ancestors to walk upright	3.9E+06
16	Homo erectus appears	1.8E+06
17	Anatomically modern humans appear	1.5E+04
18	Invention of writing	6300
19	Pyramids built in Egypt	4600
20	Voyage of Christopher Columbus	508

3. The data set "important events in the history of life" as found in the Encyclopedia Britannica?

2Oxygen begins to accumulate in atmosphere2.5E+093Oldest eukaryotic fossils2.1E+094Simple multicellular organisms evolve7.0E+085Plants colonize land4.2E+086Amphibians appear3.7E+087First insects3.6E+088Reptiles appear3.4E+089Mass extinction2.8E+0810First dinosaurs and mammals2.3E+0811Birds evolve from reptiles2.0E+0812First flowering plants1.4E+0813Mass extinction6.6E+0714Ice age2.4E+0615Advent of modern humans1.0E+05		Milestone	Years ago
3 Oldest eukaryotic fossils2.1E+094 Simple multicellular organisms evolve7.0E+085 Plants colonize land4.2E+086 Amphibians appear3.7E+087 First insects3.6E+088 Reptiles appear3.4E+089 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	1	Oldest prokaryotic fossils	3.5E+09
4 Simple multicellular organisms evolve7.0E+085 Plants colonize land4.2E+086 Amphibians appear3.7E+087 First insects3.6E+088 Reptiles appear3.4E+089 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	2	Oxygen begins to accumulate in atmosphere	2.5E+09
5Plants colonize land4.2E+086Amphibians appear3.7E+087First insects3.6E+088Reptiles appear3.4E+089Mass extinction2.8E+0810First dinosaurs and mammals2.3E+0811Birds evolve from reptiles2.0E+0812First flowering plants1.4E+0813Mass extinction6.6E+0714Ice age2.4E+0615Advent of modern humans1.0E+05	3	Oldest eukaryotic fossils	2.1E+09
6 Amphibians appear3.7E+087 First insects3.6E+088 Reptiles appear3.4E+089 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	4	Simple multicellular organisms evolve	7.0E+08
7 First insects3.6E+088 Reptiles appear3.4E+089 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	5	Plants colonize land	4.2E+08
8 Reptiles appear3.4E+089 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	6	Amphibians appear	3.7E+08
9 Mass extinction2.8E+0810 First dinosaurs and mammals2.3E+0811 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	7	First insects	3.6E+08
10First dinosaurs and mammals2.3E+0811Birds evolve from reptiles2.0E+0812First flowering plants1.4E+0813Mass extinction6.6E+0714Ice age2.4E+0615Advent of modern humans1.0E+05	8	Reptiles appear	3.4E+08
11 Birds evolve from reptiles2.0E+0812 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	9	Mass extinction	2.8E+08
12 First flowering plants1.4E+0813 Mass extinction6.6E+0714 Ice age2.4E+0615 Advent of modern humans1.0E+05	10	First dinosaurs and mammals	2.3E+08
13 Mass extinction $6.6E+07$ 14 Ice age $2.4E+06$ 15 Advent of modern humans $1.0E+05$	11	Birds evolve from reptiles	2.0E+08
14 Ice age2.4E+0615 Advent of modern humans1.0E+05	12	First flowering plants	1.4E+08
15 Advent of modern humans1.0E+05	13	Mass extinction	6.6E+07
	14	Ice age	2.4E+06
16 Present	15	Advent of modern humans	1.0E+05
	16	Present	0

4. A "timeline for the evolution of life on earth" as given in the web site of the Educational Resources in Astronomy and Planetary Science (ERAPS), University of Arizona.

	Milestone	Years ago
1	No life; shallow seas	4.0E+09
2	Origin of simple cells	3.8E+09
3	Origin of cyanobacteria	3.5E+09
4	Oxygen accumulates in atmosphere	2.5E+09
5	Protists and green algae	1.7E+09
6	Simple multicellular life (sponges, seaweeds)	1.0E+09
7	More invertebrates (flatworms, jellyfish)	7.0E+08
8	Early animals with hard parts in oceans	5.2E+08
9	Planets invade land	4.1E+08
10	Vertebrates invade land	3.5E+08
11	Coal forming forests, amphibians, BIG insects	3.0E+08
12	Mass extinction (trilobites)	2.3E+08
13	Pangaea, first mammals, first reptiles	2.0E+08
14	Mass extinction (including dinosaurs)	6.5E+07
15	Small mammals, humanoids	3.0E+07
16	Early Humans	2.0E+06
17	Us	0

5. The milestones below have been kindly provided by Paul D. Boyer, biochemist, Nobel Prize 1997.[11] The precise dates have been assigned by the author. The last two milestones have been ignored as futuristic.

	Milestone	Years ago
1	Big bang	1.5E+10
2	Solar system forms	4.8E+09
3	Earth forms	4.6E+09
4	Nitrogen atmosphere (for winds) is present or acquired	4.0E+09
5	Abundant water is present or acquired	3.9E+09
6	Organic precursors for life forms accumulate in special environment	3.9E+09
7	Primitive living organisms arise or (less likely) come from space	3.9E+09
8	Land temperature stabilizes so that most of the water is liquid	3.5E+09
9	Some life forms get energy from oxidation reduction reactions	3.2E+09
10	Organisms evolve to gain many present biochemical characteristics	3.0E+09
11	Photosynthetic capacity is acquired, and oxygen evolution begins	2.7E+09
12	Land surfaces form and plate tetonics established	2.6E+09
13	Evolution produces organisms that can use oxygen to make ATP	2.4E+09
14	Abundant microorganisms colonize the entire earth.	2.1E+09
15	Multicellular organisms arise with increased capacity for structural differentiation	7.0E+08
16	Primitive plant forms begin to evolve stems, roots, and leaves	4.0E+08
17	First humans	2.6E+06
18	Widespread use of stone tools	1.7E+06
19	Acquisition of spoken language	1.0E+06
20	Acquisition of written language	5000
21	They learn that knowledge comes from observation and experiment (scientific method)	500
22	Ability to control nature gives rise to a human population explosion	200
23	The above abilities give rise to a remarkable understanding of nature	100
24	Human activities devastate species and the environment	
25	Humans disappear geological forces and evolution continue	—

6. The data set below represents "major events in the Universe history" as published in *Scientific American* by John D. Barrow and Joseph Silk.[12]

	Milestone	Years ago
1	Big Bang	2.00E+10
2	Galaxies begin to form	1.85E+10
3	Galaxies begin to cluster	1.70E+10
4	Our protogalaxy collapses; first stars form	1.60E+10
5	Quasars are born; Population II stars form	1.50E+10
6	Population I stars form	1.00E+10
7	Our parent interstellar cloud forms	4.80E+09
8	Collapse of protosolar nebula	4.70E+09
9	Planets form; rock solidifies	4.60E+09
10	Intense cratering of planets	4.30E+09
11	Oldest terrestrial rocks form	3.90E+09
12	Microscopic life forms	3.00E+09
13	Oxygenrich atmosphere develops	2.00E+09
14	Macroscopic life forms	1.00E+09

15	Earliest fossil record	6.00E+08
16	First fishes	4.50E+08
17	Early land plants	4.00E+08
18	Ferns, conifers	3.00E+08
19	First mammals	2.00E+08
20	First birds	1.50E+08
21	First primates	6.00E+07
22	Mammals increase	5.00E+07
23	Homo sapiens	1.00E+05

7. The milestones below appear in Jean Heidmann's book Cosmic Odyssey.[13]

	Milestone	Years ago
1	Big Bang, etc.	1.5E+10
2	Age of most distant galaxies	8.0E+09
3	Formation of the Sun and the Earth	4.5E+09
4	First bacteria	3.5E+09
5	First eucaryotic organisms	1.5E+09
6	Explosion of life in the Cambria era	5.0E+08
7	The dawn of Australopithecus	3.5E+08
8	Homo habili uses tools	2.5E+08
9	Homo erectus masters the use of fire	1.0E+08
10	Invention of writing	4.0E+04
11	Eratosthenes measures the size of the Earth	2000
12	Copernicus, Galileo	400

8. The data set below is taken from a table "illustrating the temporal distribution of major events in the history of life." The table is found in a volume that makes accessible the proceedings of the 1991 Symposium "Major Events in the History of Life" convened by the IGPP Center for the Study of Evolution and the Origin of Life at the University of California, Los Angeles.[5]

_	Milestone	Years ago
	Formation of the Earth	4.6E+09
2	Origin of Life on Earth	4.0E+09
3	Formation of the oldest rocks known on Earth	3.8E+09
4	Date of oldest fossils and stromatolites	3.5E+09
5	Abundant cyanobacteria and stromatolites	2.8E+09
6	Abundant iron formations	2.5E+09
7	Latest detrital uraninite/pyrite	2.1E+09
8	Atmospheric oxygen	1.9E+09
9	Nucleated cells (phytoplankton)	1.8E+09
10	Complex (sexual) phytoplankton	1.1E+09
11	Seaweeds and protozoans	8.5E+08
12	Animals without backbones	6.0E+08
13	Fish	5.0E+08
14	Land plants and animals	4.0E+08
15	Coal swamps	3.0E+08

16 Dinosaurs and birds	2.0E+08
17 Flowering plants	1.0E+08
18 Humans	2.0E+06

9. The data set below is compiled from tables in "Major Events in the History of Mankind" by Phillip V. Tobias, Director, Palaeo-anthropology Research Unit, Department of Anatomy and Human Biology, University of the Witwatersrand, Johannesburg, South Africa.[14]

1Divergence of orangutan lineage from Hominoidea1.6E+072Divergence of gorilla from other African hominoids7.5E+063Uplift, cooling, and aridification of Africa6.0E+064Chimpanzeehominid divergence, inferred appearance of Hominidae5.7E+065"Messinian crisis", the drying up of the Mediterranean / Spread of African savannah / etc.5.5E+066Earliest known fossils identifiable as probable hominid4.8E+067Earliest fossil evidence of hominid bipedalism3.8E+068Hominid fossils known2.8E+069Differentiation of postulated "derived A. africanus"2.7E+0610One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains.2.6E+0611Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents)2.3E+0612Earliest modern human brain form; earliest signs of marked brain enlargement in hominids.2.0E+06
 3 Uplift, cooling, and aridification of Africa 4 Chimpanzeehominid divergence, inferred appearance of Hominidae 5.7E+06 5 "Messinian crisis", the drying up of the Mediterranean / Spread of African savannah / etc. 6 Earliest known fossils identifiable as probable hominid 7 Earliest fossil evidence of hominid bipedalism 8 Hominid fossils known 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest modern human brain form; earliest signs of marked brain enlargement in
 4 Chimpanzeehominid divergence, inferred appearance of Hominidae 5.7E+06 5 "Messinian crisis", the drying up of the Mediterranean / Spread of African savannah / etc. 6 Earliest known fossils identifiable as probable hominid 7 Earliest fossil evidence of hominid bipedalism 8 Hominid fossils known 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
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 6 Earliest known fossils identifiable as probable hominid 7 Earliest fossil evidence of hominid bipedalism 8 Hominid fossils known 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
 7 Earliest fossil evidence of hominid bipedalism 8 Hominid fossils known 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
 8 Hominid fossils known 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
 9 Differentiation of postulated "derived A. africanus" 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in 2.7E+06 2.6E+06 2.3E+06 2.1E+06
 10 One or more splittings of hominid lineage; earliest known Australopithecus boisei fossils; earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
 earliest known stone cultural remains. 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
 11 Acquisition of spoken language (as here inferred); many changes in mammalian fauna of Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents) 12 Earliest known Homo habilis fossils 13 Earliest modern human brain form; earliest signs of marked brain enlargement in
Africa (baboons, elephants, pigs, bovids, hippopotami, sabertoothed cats, rodents)2.3E+0612 Earliest known Homo habilis fossils2.1E+0613 Earliest modern human brain form; earliest signs of marked brain enlargement in2.1E+06
12 Earliest known Homo habilis fossils2.1E+0613 Earliest modern human brain form; earliest signs of marked brain enlargement in
13 Earliest modern human brain form; earliest signs of marked brain enlargement in
hominide 2 0E+06
10mmus. 2.0E+00
14 Movement of hominids from Africa to Asia and Europe1.8E+06
15 Emergence of Homo erectus 1.7E+06
16 Acquisition of fire by H. erectus 1.3E+06
17 Extinction of robust and hyperrobust australopithecines1.2E+06
18 Emergence of Homo sapiens5.0E+05
19 Earliest known "anatomically modern Homo sapiens"1.1E+05
20 Earliest burial of the dead 1.0E+05
21 Emergence of "modern human culture)4.0E+04
22 Earliest rock art; earliest protowriting3.5E+04
23 Earliest writing5000

10. The milestones below represent a "timeline for major events in the history of life on earth" as given by David R. Nelson, Department of Biochemistry at the University of Memphis, Tennessee.[15]

Milestone	Years ago
1 Planet earth forms	4.5E+09
2 Planet surface cools and bombardment from space slows, so life has the possibil	lity
of existing on the planet. Oldest earth rocks dated by radioactivity.	4.0E+09
3 Evidence for life seen in Greenland rocks enriched in C12 isotope. Prokaryotes	diverge
from archaea. Chlorophyll and photosynthesis evolve in the bacterial lineage	e. 3.9E+09
4 First banded iron formation seen. Implies oxygen made by photosynthesis	3.7E+09
5 First stromatolites seen.	3.5E+09

6	First tentative evidence of a eukaryotic microfossil	2.1E+09
7	Oxygen begins to rise in the atmosphere after oxygen sinks saturated.	2.0E+09
8	Oxygen level in the atmosphere reaches present day level and stabilizes. More	
	convincing evidence of eukaryotic microfossils. Chloroplasts and mitochondria present.	1.5E+09
9	Major eukaryotic phyla diverge. Plants branched before animals/fungi	1.2E+09
10	Invertebrates and vertebrates diverge. Hox gene cluster exists.	6.0E+08
11	Cambrian explosion of fossil record.	5.3E+08
12	Fish and other vertebrates diverge. Plants and fungi invade the land	4.0E+08
13	Vertebrates move onto land	3.8E+08
14	Gymnosperms (naked seed plants) diverge from angiosperms (flowering plants)	3.6E+08
15	Birds and other vertebrates diverge.	3.0E+08
16	Monocots diverge from dicots, oldest angiosperm fossil	1.8E+08
17	Oldest angiosperm fossil	1.4E+08
18	Last common ancestor of all polymorphism sequences	6.0E+07
19	Chimpanzees and humans diverge	5.0E+06
20	Homo sapiens	1.7E+06
21	Last common ancestor of all human mitochondrial DNA types	2.0E+05
22	Modern humans	5.9E+04

11. The milestones below have been compiled from information in *The First Humans: Human Origins and History to 10,000 BC*, edited by Goran Burenhult.[16]

	Milestone	Years ago
1	Purgatorius	6.0E+07
2	Petrolemuridae	5.5E+07
3	Adapiformes, omomylformes	4.5E+07
4	Aegyptopithecus, Propliapithecus, Oligopithecus, Catopithecus	4.0E+07
5	Afrotarsius	3.8E+07
6	Omomylformes, Branisella	2.7E+07
7	Prohylobates, Micropithecus, Afropithecus Proconsul	1.8E+07
8	Kenyopithecus, Dryopithecus	1.5E+07
9	Krishnapithecus	1.1E+07
10	Sivapithecus	1.0E+07
11	Ouranopithecus	9.5E+06
12	Samburu maxilla	6.5E+06
13	Gigantopithecus	5.0E+06
14	Orangutans, emergence of stone tools	1.8E+06
15	Appearance of the erectines	1.5E+06
16	Acheulian technology	6.3E+05
17	Homo erectus	5.5E+05
18	Homo heidelbergensis	3.5E+05
19	Control of fire	2.3E+05
20	Homo sapiens, modern humans	2.0E+05
21	Neanderthalis	1.3E+05
22	Mousterian technology	7.0E+04
23	Art	3.5E+04

12. The data set below is adapted from a chart on Human Evolution based on the book *From Lucy to Language*.[17]

	Milestone	Years ago
1	Ardipithecus ramidus	4.4E+06
2	Australopithecus anamensis	4.2E+06
3	Australopithecus afarensis	3.9E+06
4	Australopithecus africanus	2.8E+06
5	Australopithecus aethiopicus	2.7E+06
6	Homo sp?	2.5E+06
7	Homo rudolfensis	2.4E+06
8	Australopithecus boisei	2.3E+06
9	Homo habilis / Australopithecus habilis	1.9E+06
10	Homo ergaster	1.8E+06
11	Homo erectus	1.2E+06
12	Homo heldelbergensis	6.0E+05
13	Homo neanderthalensis	3.0E+05
14	Homo sapiens	1.0E+05

13. The milestones below have been compiled by the author and are influenced to some extent by the preceding twelve sets. In bold I highlight the main feature of each milestone.

	Milestone	Years ago
1	Big Bang / quarks / protons & neutrons / atoms of elements	1.5E+10
2	First stars	1.2E+10
3	First planets / rock solidification / solar system	4.6E+09
4	First life / cooling of Earth / formation of first rocks / water forms	3.8E+09
5	First multicelluar life (sponges, seaweeds)	1.0E+09
6	Cambrian explosion / invertebrates / vertebrates	5.3E+08
7	First mammals	2.0E+08
8	First primates / asteroid collision	6.5E+07
9	First orangutan	1.7E+07
10	First hominids	6.0E+06
11	First stone tools	2.6E+06
12	Development of speech / Homo sapiens	1.0E+06
13	Discovery of fire / hunting gathering society	5.0E+05
14	Emergence of "modern humans" / earliest burial of the dead / agrarianpastoral	
	/ sociocultural systems	1.0E+05
15	Rock art / ptotowriting	3.5E+04
16	Agriculture / prehistoric nomadic bands / techniques for starting fire	1.0E+04
17	Discovery of the wheel / writing / archaic empires / large civilizations / Egypt	
	/ Mesopotamia	5000
18	Democracy / city states / Greeks / Buddha	2500
19	Christianity	2000
20	Gunpowder	675
21	Renaissance (printing press) / discovery of new world / the scientific method	500
22	Industrial revolution (steam engine) / political revolutions (French, USA)	225
23	Modern physics / radio / electricity / automobile / airplane / capitalism & colonialism	100
24	DNA / transistor / nuclear energy / W.W.II / cold war / sputnik	50
25	Internet / human genome sequenced	5

APPENDIX B

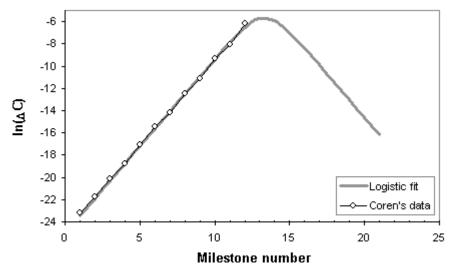
The milestones below appear in Richard L. Coren's book *The Evolutionary Trajectory*.[8] He refers to them as "critical transitions in evolution on Earth".

		Years ago
	Milestone	(centered)
1	Big Bang	1.5E+10
2	Solidification of Earth Prokaryotic life	3.5E+09
3	Eukaryotic radiation	7.5E+08
4	Appearance of class Mammalia	1.75E+08
5	Appearance of superfamily Hominoidea	3.25E+07
6	Appearance of family Hominidae	7.0E+06
7	Appearance of genus Homo	1.75E+06
8	Appearance of archaic Homo sapiens	2.5E+05
9	Appearance of H. sapiens sapiens	7.0E+04
10	Development of communal villages	1.5E+04
11	Development of writing	4000
12	Development of printing	695 [*]
13	Development of digital electronics and computing	195 [*]
* Tł	nese dates are taken with respect to calendar year 2140	

Appendix B Table I - Fit Results

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Formula fit	α	Μ	Xo	R	Ave. % deviation
$\frac{M\alpha}{(1+e^{-\alpha(X-Xo)})/(1+e^{\alpha(X-Xo)})}$	1.567	0.0092	12.83	0.99956	1.33

The correlation coefficient **R** and the average percent deviation are given as measures of the fit goodness (no estimates for χ^2 possible).



Complexity per Milestone in Coren's Data

Appendix B Figure 1. Logistic fit to the data of Coren. The vertical axis depicts the logarithm of the change in complexity. The units of complexity are arbitrary and different from those in Figures 3-5.

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